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## Multicomponent Polyanions.

# 28. The Structure of $\mathrm{K}_{7} \mathrm{Mo}_{8} \mathrm{~V}_{5} \mathrm{O}_{\mathbf{4 0}} \sim \sim \mathbf{8 \mathrm { H } _ { 2 } \mathrm { O }}$, a Compound Containing a Structurally New Potassium-Coordinated Octamolybdopentavanadate Anion 

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#### Abstract

The crystal structure of $\mathrm{K}_{7} \mathrm{Mo}_{8} \mathrm{~V}_{5} \mathrm{O}_{40} . \sim 8 \mathrm{H}_{2} \mathrm{O}$ has been determined from X-ray diffraction data collected with a Syntex $P 2_{1}$ automatic four-circle diffractometer and Mo $K \alpha$ radiation. The monoclinic ( $P 2 / / n$ ) unit cell has $a=19.435$ (4), $b=20.237$ (5), $c=12.769$ (3) $\AA$, $\beta=108 \cdot 29$ (2) ${ }^{\circ}, Z=4$. The structure was refined to $R$ 0.070 based on 7418 independent reflexions. The structure is built up from $\left[\mathrm{Mo}_{8} \mathrm{~V}_{5} \mathrm{O}_{40}\right]^{7-}$ anions which are linked together by $\mathrm{K}^{+}$ions and water molecules in a three-dimensional framework. The anion consists of edge-sharing $\mathrm{MoO}_{6}$ octahedra forming an eight-membered ring in a two-up-two-down fashion. $\mathrm{VO}_{5}$ trigonal bipyramids fill the gaps between the pairs of octahedra, and the fifth V atom is found in a $\mathrm{VO}_{4}$ tetrahedron in the center of the anion, which within


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experimental error possesses $\overline{4}$ symmetry. For edgesharing polyhedra the Mo-Mo distances vary between 3.302 (2) and 3.377 (2) $\AA$, and the Mo-V distances between 3.426 (3) and 3.524 (3) $\AA$. The Mo-O distances within the octahedra are 1.680(11)2.386 (10) $\AA$. The $\mathrm{VO}_{5}$ trigonal bipyramids all have one extremely long $\mathrm{V}-\mathrm{O}$ distance ( $>2.7 \AA$ ). There is a $\mathrm{K}^{+}$ion situated in the large void at each of the two sides of the anion ring, coordinating eight anion O atoms which form a bi-peaked hexagonal pyramid. The remaining five $\mathrm{K}^{+}$ions all coordinate $5-8$ anion and water O atoms.

## Introduction

The interpretation of data from potentiometric EMF measurements in the system $\mathrm{H}^{+}-\mathrm{MoO}_{4}^{2-}-\mathrm{HVO}_{4}^{2-}$ is difficult due to the formation of several different © 1980 International Union of Crystallography
polynuclear complexes (Pettersson, 1979). To clarify and support the results from these studies, crystallization experiments followed by X-ray structure investigations were started. The difficulty of the interpretation of EMF data was explained, as these experiments yielded a number of different phases with $\mathrm{Mo} / \mathrm{V}$ ratios between 4:8 and 10:3 (Björnberg, 1980). Since more than one of these can crystallize from the same starting solution, the great abundance of reports of various molybdovanadates in early literature is easily understood (Mellor, 1964).

More recent investigations of molybdovanadates are scarce. Heteropolyanions containing $\mathrm{P}^{\mathrm{v}}$ and $\mathrm{V}^{\mathrm{v}}$ as well as $\mathrm{Mo}^{\mathrm{VI}}$ or $\mathrm{W}^{\mathrm{VI}}$ have been thoroughly investigated (Weakley, 1974, and references therein), but among all-metal heteropolyvanadates only a limited number have been studied. Before the present series of investigations, the structurally known heteropolyvanadates with pentavalent V , not containing $\mathrm{P}^{\mathrm{v}}$, belonged to one of three types: $\mathrm{V}_{x} M_{13-x} \mathrm{O}_{40}$ (Nishikawa, Kobayashi \& Sasaki, 1975a, M=W), $\mathrm{V}_{x} M_{6-x} \mathrm{O}_{19}$ (Nishikawa, Kobayashi \& Sasaki, 1975b, $M=\mathrm{W}$ ) or $M V_{13 / 14} \mathrm{O}_{38 / 40}$ (Evans \& Konnert, 1978, $M=\mathrm{Al}, \mathrm{Mn}$ or Ni$)$.

The object of this study is the structure of $\mathrm{K}_{7} \mathrm{Mo}_{8} \mathrm{~V}_{5} \mathrm{O}_{40} \cdot \sim 8 \mathrm{H}_{2} \mathrm{O}$, which is not a Keggin (1934) structure although the composition is correct for a Keggin anion. There is no earlier report of an 8:5 molybdovanadate; the closest is a 13:8 complex (Isenburg, 1901).

## Experimental

## Crystal preparation, analysis and data

In a typical preparation 3.60 g of $\mathrm{MoO}_{3}$ was dissolved in 50 ml of hot 0.50 M KOH , and 5.85 g of $\mathrm{NH}_{4} \mathrm{VO}_{3}$ was dissolved in 60 ml of hot water. The vanadate solution was poured into the molybdate solution and 12.5 ml of $2 M \mathrm{HCl}$ added. 7.46 g of KCl was dissolved in this solution, which was filtered at about 313 K . Overnight, yellow acicular crystals, growing in thistle-like arrangements, were formed. The crystals are mechanically fragile as well as unstable in air, and during the X-ray exposures they were sealed, with part of the mother liquor, in a Lindemann-glass

Table 1. Crystal data for $\mathrm{K}_{7} \mathrm{Mo}_{8} \mathrm{~V}_{5} \mathrm{O}_{40} \sim \sim 8 \mathrm{H}_{2} \mathrm{O}$
Monoclinic, space group $P 2_{1} / n$ (No. 14)

| $a=19.435(4) \AA$ | $M_{r}=2079.07$ |
| :--- | :--- |
| $b=20.237(5)$ | $D_{x}=2 \cdot 896 \mathrm{Mg} \mathrm{m}^{-3}$ |
| $c=12 \cdot 769(3)$ | $D_{m}=2.89(1)$ |
| $\beta=108 \cdot 29(2)^{\circ}$ | $\mu(\mathrm{Mo} \mathrm{Ka})=3.692 \mathrm{~mm}^{-1}$ |
| $Z=4$ |  |

$a=19.435$ (4) $\AA$
$M_{r}=2079.07$
$c=12 \cdot 769(3)$
$D_{m}=2.89(1)$
$Z=4$
$V=4768.4 \AA^{3}$
capillary. Water analysis was performed by heating on a thermobalance and gave $6.9 \mathrm{wt} \% \mathrm{H}_{2} \mathrm{O}$ (calculated for $8 \mathrm{H}_{2} \mathrm{O}: 6.9 \mathrm{wt} \%$ ).

From Weissenberg and precession photographs the crystals were found to be monoclinic, and systematic extinctions $0 k 0: k=2 n+1$ and $h 0 l: h+l=2 n+1$ uniquely determined the space group as $P 2_{1} / n$. The density was determined by flotation in a diiodomethane/chloroform solution. Crystal data are given in Table 1.

## Data collection and reduction

A crystal $0.3 \times 0.18 \times 0.10 \mathrm{~mm}$ was chosen. The data were collected at the Department of Inorganic Chemistry, University of Göteborg, and Chalmers University of Technology, Göteborg, on a Syntex $P 2_{1}$ automatic four-circle diffractometer with graphitemonochromatized Mo $K \alpha$ radiation ( $\lambda=0.71069 \AA$ ). The cell parameters were determined by least squares from the setting angles for 15 reflexions.

In the collection of intensities the $\theta / 2 \theta$ scan method was used, and the $2 \theta$ scan speed was allowed to vary between 2 and $8^{\circ} \mathrm{min}^{-1}$ depending on the intensity of the measured reflexion.

11467 independent reflexions were collected in the region $(\sin \theta) / \lambda<0.65 \AA^{-1}$. No separate background measurements were made during the data collection. A profile analysis based on the Lehmann \& Larsen (1974) method was instead applied to the 96 -step profile measured for each reflexion (program LELA; Lindqvist \& Ljungström, 1979). Correction was made for Lorentz and polarization effects. 7418 reflexions with $F_{o}^{2} \geq 3 \sigma\left(F_{o}^{2}\right)$ were considered observed and were used in the subsequent calculations. Absorption correction was applied with an $8 \times 6 \times 4$ Gaussian grid [ $\mu(\mathrm{Mo} \mathrm{K} \mathrm{K} \alpha)=3.692 \mathrm{~mm}^{-1}$ ] and the transmission factor varied between 0.576 and 0.699 .

## Structure determination and refinement

The structure was solved with MULTAN (Germain, Main \& Woolfson, 1970). The 214 reflexions with $E \geq 2.50$ were used for sign determination with the $\sum_{2}$ relationship. A basis set consisting of seven reflexions was used: one determined by the $\sum_{1}$ formula, three for definition of the origin and three being varied in the MULTAN procedure. The E maps based on the set with the best figures of merit revealed all eight Mo atoms, and heavy-atom methods gave the positions of all the other non-hydrogen atoms. Block-matrix leastsquares refinement with isotropic temperature factors gave $R=0.099$ which decreased to 0.073 when anisotropic temperature factors were applied. In a difference synthesis calculated at this stage a number of peaks corresponding to an electron density of about
$2.5 \mathrm{e} \AA^{-3}$ or less could be found. Most of these appeared in positions situated at very reasonable hydrogen-bond and $\mathrm{K}-\mathrm{O}$ bond distances from atoms already included in the model. A refinement of the occupancy factors of 14 water O atom positions was performed, but did not give chemically significant results. Consequently, only nine of the probable water O atom positions were included in the final model, with no attempt to determine the occupancy factor of each position (which was set equal to one). Moreover, $\mathrm{K}(7)$ appears to be distributed between two positions, $\mathrm{K}(7)$ and $\mathrm{K}(7)^{\prime \prime}$. A refinement of the occupancy factors of these two positions gave 0.53 (2) and 0.44 (2) respectively. The occupancy factors were therefore set at 0.55 and 0.45 , making the sum equal to 1 . Refinement finally converged at $R=0.070$ ( $R_{w}=0.073$ ), with $R=\sum| | F_{o}\left|-\left|F_{c}\right|\right| / \sum\left|F_{o}\right|$ and $R_{w}=\left[\sum w\left(\left|F_{o}\right|-\left|F_{c}\right|\right)^{2} / \sum w\left|F_{o}\right|^{2}\right]^{1 / 2} . \sum w\left(\left|F_{o}\right|-\left|F_{c}\right|\right)^{2}$ was minimized.

In the final cycle the parameter shifts were less than $0 \cdot 08 \sigma . \mathrm{Mo}^{3+}, \mathrm{V}^{2+}, \mathrm{K}^{+}, \mathrm{O}^{-}$(anion O atoms) and O scattering factors were used and account was taken of the real and imaginary parts of the anomalous-disper-
sion correction (International Tables for X-ray Crystallography, 1974). The computer programs were those provided with the Syntex $R 3$ Crystallographic System, the Data General NOVA3 computer of which was also used for the computations.

Final atomic positional parameters are given in Table 2.*

## Description and discussion of the structure

The structure is built up from $\left[\mathrm{Mo}_{8} \mathrm{~V}_{5} \mathrm{O}_{40}\right]^{7-}$ anions (Figs. 1 and 2). These anions contain eight $\mathrm{MoO}_{6}$ octahedra which share edges in a two-up-two-down fashion to form a puckered ring of octahedron pairs. $\mathrm{VO}_{5}$ trigonal bipyramids are fitted in by sharing two edges of the same pyramid with the $\mathrm{MoO}_{6}$ octahedra. These twelve metal atoms thus form two six-membered

[^0]Table 2. The fractional atomic coordinates ( $\times 10^{4}$; for Mo and $\mathrm{V} \times 10^{5}$ )
Numbers and letters in the O atom designation denote the metal atom(s) to which each O atom is coordinated.

|  | $x$ | $y$ | $z$ |  | $x$ | $y$ | $z$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Mo(1) | 77199 (6) | 12102 (6) | 31837 (9) | O(67c) | 7040 (6) | 3241 (5) | 6426 (8) |
| $\mathrm{Mo}(2)$ | 85517 (7) | 23813 (6) | 22355 (10) | O(67d) | 6400 (5) | 2309 (4) | 5216 (8) |
| $\mathrm{Mo}(3)$ | 96451 (6) | 33329 (6) | 42358 (10) | O(7) | 8012 (7) | 2443 (6) | 7933 (9) |
| $\mathrm{Mo}(4)$ | 87428 (7) | 44550 (6) | 51752 (10) | $\mathrm{O}^{\prime}(7)$ | 6604 (6) | 2204 (6) | 7539 (9) |
| $\mathrm{Mo}(5)$ | 69602 (7) | 44099 (6) | 39207 (10) | O(78d) | 7337 (5) | 1436 (5) | 6482 (8) |
| Mo (6) | 61072 (7) | 32492 (6) | 48934 (10) | $\mathrm{O}(78 \mathrm{e})$ | 7943 (5) | 2345 (4) | 5674 (7) |
| $\mathrm{Mo}(7)$ | 72328 (8) | 23284 (7) | 68964 (11) | $\mathrm{O}(8)$ | 8865 (5) | 1398 (5) | 7058 (8) |
| $\mathrm{Mo}(8)$ | 81329 (7) | 12136 (6) | 59574 (10) | $\mathrm{O}^{\prime}(8)$ | 8090 (6) | 0382 (5) | 5962 (9) |
| V (a) | 94627 (12) | 16119 (11) | 46884 (19) | $\mathrm{O}(18 a)$ | 8600 (5) | 1315 (5) | 4798 (7) |
| V (b) | 81257 (13) | 40644 (11) | 23431 (19) | $\mathrm{O}(18 d)$ | 7233 (5) | 1284 (4) | 4325 (7) |
| V (c) | 76200 (18) | 40017 (15) | 67020 (25) | $\mathrm{O}(\mathrm{a})$ | 9966 (5) | 1777 (6) | 5926 (8) |
| $\mathrm{V}(\mathrm{d})$ | 63533 (12) | 15400 (11) | 44419 (18) | $\mathrm{O}^{\prime}(a)$ | 9864 (6) | 1022 (6) | 4226 (9) |
| V (e) | 78930 (11) | 28212 (10) | 45633 (17) | $\mathrm{O}(\mathrm{b})$ | 7400 (6) | 3869 (6) | 1363 (9) |
| $\mathrm{O}(1)$ | 6982 (5) | 1361 (5) | 2059 (8) | $\mathrm{O}^{\prime}($ b $)$ | 8564 (6) | 4618 (5) | 1845 (9) |
| $\mathrm{O}^{\prime}(1)$ | 7828 (6) | 0384 (5) | 3194 (9) | $\mathrm{O}(\mathrm{c})$ | 8374 (8) | 3812 (8) | 7630 (10) |
| $\mathrm{O}(12 \mathrm{a})$ | 8492 (5) | 1478 (4) | 2644 (8) | $\mathrm{O}^{\prime}(\mathrm{c})$ | 7272 (8) | 4569 (7) | 7258 (12) |
| $\mathrm{O}(12 e)$ | 7846 (5) | 2349 (4) | 3436 (7) | $\mathrm{O}(\mathrm{d})$ | 5846 (6) | 1694 (5) | 3186 (8) |
| $\mathrm{O}(2)$ | 7770 (6) | 2456 (5) | 1181 (7) | $\mathrm{O}^{\prime}($ d $)$ | 5965 (6) | 0954 (5) | 4925 (9) |
| $\mathrm{O}^{\prime}(2)$ | 9186 (6) | 2296 (5) | 1600 (9) | K(1) | 5752 (2) | 0589 (2) | 1725 (3) |
| $\mathrm{O}(23 \mathrm{a})$ | 9378 (5) | 2406 (4) | 3914 (7) | K(2) | 6372 (2) | 2760 (2) | 1966 (3) |
| $\mathrm{O}(23 \mathrm{~b})$ | 8668 (5) | 3306 (4) | 2687 (7) | K(3) | 9427 (2) | 2770 (2) | 7174 (3) |
| $\mathrm{O}(3)$ | 10208 (5) | 3232 (5) | 5549 (8) | K(4) | 6733 (4) | -0271 (3) | 5456 (5) |
| $\mathrm{O}^{\prime}(3)$ | 10226 (6) | 3422 (5) | 3494 (9) | K(5) | 9583 (4) | 0871 (4) | 1872 (7) |
| O(34b) | 9345 (5) | 4229 (5) | 4279 (8) | K(6) | 8204 (5) | 6525 (4) | 5291 (5) |
| $\mathrm{O}(34 \mathrm{e})$ | 8658 (5) | 3318 (4) | 4888 (7) | K(7) | 5271 (6) | 1878 (6) | 6374 (8) |
| $\mathrm{O}(4)$ | 9323 (6) | 4300 (5) | 6446 (9) | K(7)" | 5225 (19) | 1083 (18) | 6509 (20) |
| $\mathrm{O}^{\prime}(4)$ | 8775 (6) | 5282 (5) | 5043 (9) | $\mathrm{Aq}(1)$ | 8897 (4) | -0343 (4) | 4716 (7) |
| $\mathrm{O}(45 b)$ | 7868 (5) | 4347 (4) | 3552 (7) | $\mathrm{Aq}(2)$ | 4598 (10) | 0406 (11) | 3907 (15) |
| $\mathrm{O}(45 \mathrm{c})$ | 7847 (5) | 4351 (5) | 5505 (8) | Aq(3) | 3914 (19) | 3508 (12) | 4474 (14) |
| O (5) | 6384 (5) | 4217 (5) | 2654 (8) | Aq(4) | 0098 (10) | -0378 (9) | 2897 (26) |
| $\mathrm{O}^{\prime}(5)$ | 6873 (7) | 5241 (5) | 4038 (10) | $\mathrm{Aq}(5)$ | 1135 (13) | 1043 (13) | 2971 (21) |
| $\mathrm{O}(56 \mathrm{c})$ | 6374 (6) | 4151 (5) | 4860 (9) | Aq (6) | 1261 (10) | 2110 (11) | 4718 (17) |
| $\mathrm{O}(56 e)$ | 7118 (5) | 3273 (4) | 4239 (7) | $\mathrm{Aq}(7)$ | 4468 (12) | 2034 (14) | 4497 (22) |
| O(6) | 5586 (6) | 3123 (5) | 3584 (9) | $\mathrm{Aq}(8)$ | 7121 (20) | -1600 (10) | 5465 (17) |
| $\mathrm{O}^{\prime}$ (6) | 5515 (6) | 3322 (6) | 5624 (10) | $\mathrm{Aq}(9)$ | 1654 (20) | 4329 (10) | 2687 (22) |



Fig. 1. The $\left[\mathrm{Mo}_{8} \mathrm{~V}_{5} \mathrm{O}_{40}\right]^{7-}$ anion drawn with idealized polyhedra.


Fig. 2. A stereoscopic drawing of the $\left[\mathrm{Mo}_{8} \mathrm{~V}_{5} \mathrm{O}_{40}\right]^{7-}$ anion. The thermal ellipsoids are scaled to enclose $50 \%$ probability (Johnson, 1976).
rings which are sandwiched on top of each other with a slight mutual twist. The fifth V atom is found in the center of the anion inside a $\mathrm{VO}_{4}$ tetrahedron which shares each corner with two $\mathrm{MoO}_{6}$ octahedra. The anion is unusual in that it contains no two-coordinated O atoms. All O atoms are either terminal or threecoordinated. The anions are joined in a three-dimensional framework by $\mathrm{K}^{+}$ions and hydrogen bonds from the water molecules. The closest distance between O atoms in adjacent anions is 2.97 (2) $\AA$, which implies that the anions are not in van der Waals contact with each other. The sum of two oxygen van der Waals radii is $2.8 \AA$ (Pauling, 1960).

## The $\left[\mathrm{Mo}_{8} \mathrm{~V}_{5} \mathrm{O}_{40}\right]^{7-}$ anion

The $\mathrm{MoO}_{6}$ octahedra. As is shown in Table 3, the $\mathrm{MoO}_{6}$ octahedra are noticeably distorted. The usual variation in $\mathrm{Mo}-\mathrm{O}$ lengths according to coordination number is shown quite clearly, with Mo-O distances for terminal $O$ atoms between 1.68 and $1.71 \AA$, while all the $\mathrm{Mo}-\mathrm{O}$ distances for three-coordinated O atoms are $1.90 \AA$ or longer. The long Mo-O bonds are also distributed as expected, with distances to O atoms trans to the terminal O atoms longer than $2.21 \AA$. These O atoms are, of course, situated on the octahedron edges pointing towards the center of the anion. The remaining two O atoms of each octahedron
are at intermediate distances with $\mathrm{Mo}-\mathrm{O}$ lengths between 1.90 and $1.99 \AA$. There is a slight systematic variation: when an O atom shared with a V atom is in an apical position of the $\mathrm{VO}_{5}$ trigonal bipyramid, the Mo-O distance is a few hundredths of an ångström shorter than for an O atom in an equatorial position (see below). As a whole, the configuration of O atoms around the Mo atoms is in accordance with those found in other structures (Strandberg, 1974). As in all polyanions, the metal atoms are displaced within their O atom coordination figures in a direction away from the center of the anion.

The $\mathrm{VO}_{4}$ and $\mathrm{VO}_{5}$ groups. The central $\mathrm{VO}_{4}$ tetrahedron is fairly regular. Perfectly regular $\mathrm{VO}_{4}$ tetrahedra have been found in cubic Keggin (1934) structures, and this has often been accounted for by ascribing the regularity to rotational disorder of the anion (Nishikawa, Kobayashi \& Sasaki, 1975a). This seems unlikely in the present structure, as the O atoms of the $\mathrm{VO}_{4}$ tetrahedron show no anomalies in their thermal parameters. In solution, the $\mathrm{VO}_{4}^{3-}$ anion is probably very close to regular (Tillmanns \& Baur, 1971), and the anion ring apparently makes an attractive site for a $\mathrm{VO}_{4}$ tetrahedron.

The $\mathrm{VO}_{5}$ trigonal bipyramids are similar to the same groups in the $\left(\mathrm{Mo}_{4} \mathrm{~V}_{8} \mathrm{O}_{36}\right]^{8-}$ anion (Björnberg, 1979). Four of the O atoms make up a tetrahedron showing the usual pattern (Evans, 1966) of two short and two long bonds. The fifth O atom in each group is situated a long way from the V atom, the $\mathrm{V}-\mathrm{O}$ length in all four cases being $2 \cdot 71-2 \cdot 86 \AA$. This distance is at the limit of making the five-coordination uncertain. As is the case in $\left[\mathrm{Mo}_{4} \mathrm{~V}_{8} \mathrm{O}_{36}\right]^{8-}$, the Mo-O distances for these O atoms are longer than for O atoms coordinated only to two Mo atoms. This supports the description of the V atoms as being five-coordinate. As was mentioned above, the Mo-O length for these apical (with respect to the $\mathrm{VO}_{5}$ groups) O atoms is slightly shorter than for O atoms in equatorial positions in the $\mathrm{VO}_{5}$ bipyramids, which shows the weakness of the $\mathrm{V}-\mathrm{O}$ bond of the apical O atoms.

The terminal O atoms can be divided into two distinct groups: one with the atoms pointing away from the plane of the anion ring (henceforth called 'axial' O atoms, denoted without primes) and the other with the atoms pointing from their respective metal atom in a direction parallel to the ring plane (henceforth called 'equatorial' O atoms, denoted with primes). There seems to be no systematic relation between $\mathrm{Mo}-\mathrm{O}$ (or $\mathrm{V}-\mathrm{O}$ ) length and the axial or equatorial position of the O atom.

Bond distances within the anion are given in Table 3.
The mechanism behind the formation of the $\left[\mathrm{Mo}_{8} \mathrm{~V}_{5} \mathrm{O}_{40}\right]^{7-}$ anion is not easily understood. All the V atoms have tetrahedral or near-tetrahedral coordination figures, which makes it probable that the anion is formed rapidly upon acidification of the



molybdovanadate solution. \{The $\left[\mathrm{Mo}_{4} \mathrm{~V}_{8} \mathrm{O}_{36}\right]^{8-}$ anion, which is formed if crystals of $\mathrm{K}_{7} \mathrm{Mo}_{8} \mathrm{~V}_{5} \mathrm{O}_{40} . \sim 8 \mathrm{H}_{2} \mathrm{O}$ are dissolved in water and left to crystallize (Björnberg, 1979), contains octahedrally coordinated V atoms. \}

## The potassium ions and water molecules

As usual, most of the $\mathrm{K}^{+}$ions coordinate 7-11 anion or water O atoms within a distance of $3.25 \AA$. The coordination figures are rather irregular, and the structure as a whole is probably formed by the possibility of packing the anions in an energetically favorable way and by the formation of hydrogen bonds from water molecules, rather than by bonds in


Fig. 3. A schematic drawing showing the position and coordination to the anion of the $K(2)$ ion.
preferred directions from $\mathrm{K}^{+}$ions. $\mathrm{K}(2)$ and $\mathrm{K}(3)$, however, are two exceptions to this pattern. The axial terminal O atoms of the anion form six-membered rings around the cavities on each side of the anion. $\mathrm{K}(2)$ and $\mathrm{K}(3)$ are situated near the centers of these rings, also coordinating two O atoms of the central $\mathrm{VO}_{4}$ tetrahedron (Fig. 3). The $\mathrm{K}^{+}$ions are displaced slightly outward from the plane of the axial O atoms; the distances from $K(2)$ and $K(3)$ to the least-squares planes through the O atoms are 0.601 (4) and 0.648 (4) $\AA$ respectively. The coordination around $\mathrm{K}(2)$ and $\mathrm{K}(3)$ is completed by water molecules and O atoms from neighboring anions.

It seems probable that these two $\mathrm{K}^{+}$ions are important for the stability of the anion. The $\left[\mathrm{V}_{5} \mathrm{~W}_{8} \mathrm{O}_{40}\right]^{7-}$ anion described by Nishikawa et al. (1975a) has a similar formula, but that is a Keggin anion. The present structure has not been observed for any other anion, while the Keggin structure has been

Table 4. K-O distances $(\AA)$ less than $3.4 \AA$
The superscripts refer to the following symmetry operations:

|  | (i) $x-\frac{1}{2}, \frac{1}{2}-y, z-\frac{1}{2}$ <br> (ii) $1 \frac{1}{2}-x, y-\frac{1}{2}, \frac{1}{2}-z$ <br> (iii) $\frac{1}{2}+x, \frac{1}{2}-y, \frac{1}{2}+z$ <br> (iv) $1-x,-y, 1-z$ <br> (v) $1 \frac{1}{2}-x, y-\frac{1}{2}, 1 \frac{1}{2}-z$ |  | (vi) $\frac{1}{2}+x, \frac{1}{2}-y, z-\frac{1}{2}$ <br> (vii) $1 \frac{1}{2}-x, \frac{1}{2}+y, \frac{1}{2}-z$ <br> (viii) $2-x, 1-y, 1-z$ <br> (ix) $1 \frac{1}{2}-x, \frac{1}{2}+y, 1 \frac{1}{2}-z$ |  | (x) $1-x, 1-y, 1-z$ <br> (xi) $\quad x-\frac{1}{2}, \frac{1}{2}-y, \frac{1}{2}+z$ <br> (xii) $x-1, y, z$ <br> (xiii) $\frac{1}{2}-x, \frac{1}{2}+y, \frac{1}{2}-z$. |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{K}(1)-\mathrm{O}\left(4^{\text {i }}\right.$ ) | $2 \cdot 70$ (1) | $\mathrm{K}(3)-\mathrm{O}(a)$ | $2 \cdot 95$ (1) | $\mathrm{K}(5)-\mathrm{Aq}(4)$ | $2 \cdot 88$ (2) | $\mathrm{K}(7)-\mathrm{Aq}(7)$ | 2.44 (3) |
| $\mathrm{O}^{\prime}\left(b^{\text {II }}\right.$ ) | 2.73 (1) | $\mathrm{O}(8)$ | 2.97 (1) | $\mathrm{O}(12 a)$ | $2 \cdot 88$ (2) | $\mathrm{O}^{\prime}(7)$ | 2.64 (2) |
| $\mathrm{O}^{\prime}$ (4i) | $2 \cdot 76$ (1) | $\mathrm{O}(34 e)$ | 3.04 (1) | $\mathrm{O}^{\prime}(a)$ | $2 \cdot 90$ (1) | $\mathrm{O}^{\prime}\left(2^{\text {x1 }}\right.$ ) | 2.78 (2) |
| O(1) | 2.77 (1) | $\mathrm{O}(78 e)$ | 3.04 (1) | $\mathrm{Aq}(5)$ | 2.92 (3) | $\mathrm{O}^{\prime}\left(3^{\text {xl }}\right.$ ) | 2.80 (2) |
| $\mathrm{O}\left(3^{1}\right)$ | $2 \cdot 84$ (1) | $\mathrm{O}(3)$ | 3.08 (1) | $\mathrm{O}^{\prime}(2)$ | $2 \cdot 98$ (1) | $\mathrm{O}(67 d)$ | $3 \cdot 13$ (2) |
| $\mathrm{O}(\mathrm{d})$ | $2 \cdot 88$ (1) | $\mathrm{O}(\mathrm{c})$ | $3 \cdot 12$ (2) | $\mathrm{O}^{\prime}\left(5^{11}\right)$ | 2.99 (2) | $\mathrm{O}^{\prime}(6)$ | 3.16 (2) |
| $\mathrm{O}\left(34 b^{\text {i }}\right.$ ) | $3 \cdot 02$ (1) | $\mathrm{O}(4)$ | $3 \cdot 22$ (1) | Aq( $3^{v 1}$ ) | 3.18(2) | $\mathrm{O}^{\prime}(d)$ | 3.21 (2) |
|  |  | O(7) | $3 \cdot 26$ (1) | $\mathrm{O}^{\prime}\left(6^{\mathrm{vl}}\right)$ | $3 \cdot 21$ (2) |  |  |
| $\mathrm{K}(2)-\mathrm{O}(56 e)$ | 2.99 (1) | $\mathrm{O}\left(d^{\text {iii] }}\right)$ | 2.87 (1) |  |  |  |  |
| $\mathrm{O}(12 e)$ | 3.01 (1) | $\mathrm{Aq}\left(7^{\text {iliI }}\right)$ | 2.97 (3) | $\mathrm{K}(6)-\mathrm{O}^{\prime}(4)$ | $2 \cdot 81$ (1) | $\mathrm{K}(7)^{\prime \prime}-\mathrm{O}^{\prime}\left(3^{\text {xil }}\right)$ | 2.72 (3) |
| $\mathrm{O}(\mathrm{d})$ | 3.02 (1) | $\mathrm{O}\left(6^{\text {III }}\right)$ | 3.01 (1) | $\mathrm{O}\left(2^{\text {vil }}\right)$ | 2.90 (1) | $\mathrm{Aq}(9)$ | 2.84 (5) |
| O(6) | $3 \cdot 02$ (1) |  |  | $\mathrm{O}\left(1^{\text {vlI }}\right)$ | 2.93 (1) | $\mathrm{O}^{\prime}\left(d^{\prime}\right)$ | 2.84 (3) |
| O(1) | 3.06 (1) | $\mathrm{K}(4)-\mathrm{Aq}(8)$ | 2.79 (2) | Aq( $6^{\text {vill }}$ ) | 2.95 (2) | $\mathrm{Aq}\left(2^{\text {xill }}\right.$ ) | $3 \cdot 10$ (4) |
| O(5) | 3.08 (1) | $\mathrm{O}^{\prime}\left(b^{\mathrm{iI}}\right)$ | $2 \cdot 82$ (1) | $\mathrm{O}\left(3^{\text {vill }}\right)$ | 2.96 (1) | $\mathrm{Aq}\left(7^{\text {i }}\right.$ ) | $3 \cdot 18$ (4) |
| O(2) | $3 \cdot 24$ (1) | $\mathrm{O}^{\prime}(8)$ | 2.84 (1) | $\mathrm{O}^{\prime}\left(7^{1 \times}\right)$ | 3.01 (1) |  |  |
| $\mathrm{O}(\mathrm{b})$ | $3 \cdot 25$ (1) | $\mathrm{O}^{\prime}\left(d^{\prime}\right.$ | $2 \cdot 86$ (1) | $\mathrm{Aq}\left(9^{\mathrm{x}}\right)$ | $3 \cdot 05$ (3) |  |  |
| $\mathrm{O}\left(a^{1}\right)$ | $2 \cdot 80$ (1) | $\mathrm{Aq}\left(2^{\text {lv }}\right.$ ) | 2.96 (2) |  |  | $\mathrm{K}(7)^{\prime \prime}-\mathrm{K}(7)$ | $1 \cdot 62$ (4) |
| $\mathrm{Aq}\left(6^{1}\right)$ | $2 \cdot 82$ (2) | $\mathrm{O}^{\prime}\left(c^{v}\right)$ | 2.97 (2) |  |  |  |  |
| $\mathrm{O}\left(3^{\text {i }}\right.$ ) | $3 \cdot 14$ (1) | $\mathrm{O}\left(c^{v}\right)$ | $3 \cdot 13$ (2) |  |  |  |  |

Table 5. Probable hydrogen-bond distances ( $\AA$ )
The superscripts refer to the following symmetry operations:

| (i) ${ }^{\text {(ii) }}$ (ii) $\quad x$ | $2-x,-y, 1-z$ |  | $1 \frac{1}{2}-x, \frac{1}{2}+y,-z-\frac{1}{2}$ |
| :---: | :---: | :---: | :---: |
|  | $\frac{1}{2}-y, z-\frac{1}{2}$ | (vi) $x, y, 1+z$ |  |
| (iii) 1 (iv) $1 \frac{1}{2}$ | $\frac{1}{2}-x, \frac{1}{2}+y, \frac{1}{2}-z$ | (vii) $1 \frac{1}{2}-x, y-\frac{1}{2}, \frac{1}{2}-z$. |  |
|  | $-\frac{1}{2},-z-\frac{1}{2}$ |  |  |
| $\mathrm{Aq}(1)-\mathrm{O}^{\prime}\left(a^{\text {1 }}\right.$ ) | 2.73 (2) | $\mathrm{Aq}(5)-\mathrm{O}^{\prime}(c)$ | $2.92(3)$3.06 (3) |
| $\mathrm{O}^{\prime}(1)$ | 2.78 (1) | $\mathrm{Aq}\left(6^{\text {lV }}\right.$ ) |  |
| $\mathrm{O}($ b) | 2.94 (2) | $\begin{gathered} \mathrm{Aq}(6)-\mathrm{Aq}\left(5^{v}\right) \\ \mathrm{O}(2) \end{gathered}$ |  |
| $\mathrm{O}^{\prime}(8)$ | 2.95 (2) |  | 3.06 (3) |
|  |  |  | 3.07 (2) |
| $\mathrm{Aq}(2)-\mathrm{O}^{\prime}\left(d^{\text {III }}\right)$ | 2.79 (2) | $\mathrm{Aq}(7)-\mathrm{O}\left(7^{v}\right)$ | 3.09 (3) |
| O (c) | 2.90 (2) | $\mathrm{O}\left(c^{\nu}\right)$ | $3 \cdot 16$ (3) |
| $\mathrm{Aq}(3)-\mathrm{O}\left(7^{11 \mathrm{iI}}\right)$ | 2.91 (3) | $\mathrm{Aq}(8)-\mathrm{O}\left(7^{\text {v }}\right.$ ) | 2.89 (3) |
| $\mathrm{O}^{\prime}\left(6^{\prime}\right)$ | 3.02 (4) | $\mathrm{O}\left(2^{\text {vil }}\right.$ ) | 2.90 (2) |
|  |  | $\mathrm{O}(b)$ | 2.93 (3) |
| $\mathrm{Aq}(4)-\mathrm{O}\left(5^{1}\right)$$\mathrm{O}(8)$ | 2.86 (2) | $\mathrm{O}\left(c^{\mathrm{c} 1}\right)$ | 3.00 (3) |
|  | 2.87 (2) |  |  |
| O(8) |  | $\mathrm{Aq}(9)-\mathrm{O}(78 d)$ | 2.80 (3) |
|  |  | $\mathrm{O}^{\prime}\left(c^{\mathrm{cl}}\right)$ | 3.04 (3) |

found for a number of different complexes. The two $\mathrm{K}^{+}$ ions seem to be the stabilizing agents preventing the relocation of O atoms necessary to form the more condensed structure of a Keggin anion.
All the water molecules seem to be engaged in hydrogen bonds to anion O atoms or to other water molecules. The anions are packed to form layers parallel to the $x z$ plane, with comparatively few bonds between these layers. This explains the needle-like shape and poor mechanical properties of the crystals. $\mathrm{K}-\mathrm{O}$ lengths are given in Table 4 and probable hydrogen-bond lengths in Table 5.

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[^0]:    * Lists of structure factors and anisotropic thermal parameters have been deposited with the British Library Lending Division as Supplementary Publication No. SUP 35123 ( 30 pp.). Copies may be obtained through The Executive Secretary, International Union of Crystallography, 5 Abbey Square, Chester CHl 2HU, England.

